

Remember:  
 • Focus  
 • Look again and doubt your answers  
 • Env. diagrams  
 → tuples & lists  
 → think indexing  
 → CAREFUL w/ LEXICAL/DYNAMIC

Use your brain!  
 When drawing env. diagrams, pay attention to nesting [ ]

**lambda**  
 variables defined in env. which procedure was defined  
 parent of frame is env. where it was called  
 → NONLOCAL? looks up every frame in parent instead of new var. until global → error if can't find

def make(a,b,c):  
 if a == 42:  
 return bla  
 return c  
 if c errors → error.

ALWAYS KNOW WHAT FUNCTION TAKES IN AND RETURNS  
 like (lambda x, y: x\*\*2 + y)(3, 4)  
 13

seq. append(elem)  
 seq. extend(seq)  
 seq. remove(q) → removes 'q' (first instance of it)  
 seq. pop(i) → at index i, or last elem if ()

**Object Oriented Programming**

>>> class Account (object):  
 class statement Account;  
 def \_\_init\_\_(self, holder):  
 self.balance = 0  
 self.holder = holder  
 def deposit(self, amount):  
 self.balance += amount  
 return self.balance  
 interest = 0.02  
 >>> class CheckingAccount (Account):  
 deposit\_charge = 1  
 interest = 0.01  
 def deposit(self, amount):  
 return Account.deposit(self, amount + self.deposit\_charge)

When calling need Account().  
 like: a = Account('Hiner')  
 >>> a.balance  
 >>> a.deposit(500)  
 >>> a.balance = 400  
 >>> a.deposit(500)  
 >>> a.balance = 900

INHERITANCE  
 multiple inheritance:  
 >>> class AsSeenOnTV (CheckingAccount, SavingsAccount):  
 def \_\_init\_\_(self, holder):  
 self.holder = holder  
 self.balance = 1

def take\_all(self): # prints color every time it takes  
 for i in range(len(self.skittles)):  
 it = self.skittles[i].color == color:  
 skittle = self.skittles[i]  
 self.skittles = self.skittles[i] + self.skittles[i+1:]  
 return skittle

THINK ABOUT INHERITANCE!  
 DON'T MIX UP! WHAT SELF IS IT REFERRING TO?

Huge(). medium(). small().  
 self refers to huge.

def foolist():  
 return [elem\*\*2 for elem in list if elem % 2 == 0]

**NEWTON'S METHOD / iter.improve:**

iter.improve takes in (update, done, guess=1, max\_updates=1000)  
 k=0  
 while not done(guess) and k < max\_updates:  
 guess = update(guess)  
 k += 1  
 return guess

update takes in (a), to find \_\_\_ of a (like cube root of a)  
 def update(guess): return \_\_\_ update(guess, a)  
 def done(guess): return guess + guess + guess == a  
 return iter.improve(update, done) cube root

approx\_derivative(f, x, delta 1e-5)  
 newton\_update(f) → does thing w/ slopes, returns update \* fact.  
 def find\_root(f, guess=1):  
 return iter.improve(newton\_update(f), lambda x: f(x) == 0, guess)

square-root-newton(a) finds sq. root of a:  
 return find\_root(lambda x: pow(x, 2) - a)

MT1: def invert(f):  
 def glx:  
 return find\_root(lambda y: f(y) - x)  
 return g.

def make\_derivative(f, h=1e-5):  
 def derivative(a):  
 h = 0  
 df = (f(a+h) - f(a)) / h  
 return df/h  
 return derivative

BTW...  
 SLICING DOES NOT MUTATE ORIGINAL LIST

== VS IS  
 ls = [1, 2, 3, 4]  
 list = [1, 2, 3, 4]  
 ls == list (True)  
 ls is list (False)

Map Reduce  
 input # the tempset  
 ↓  
 mapper (line cont. ↓ 'line' Py)  
 ↓  
 SORT 'line'  
 ↓ sorted →  
 reducer (sum.py) ↓ 2878  
 vals

Sets:  
 unordered, no duplicates,  
 >>> S = {3, 2, 1, 4, 4}  
 >>> S  
 {1, 2, 3, 4}

Iterators / Streams / Gen.  
 - next method: calculates next val, checks if any vals left  
 - iter method: returns another if object has both next & iter, iter only returns self

Generators are special kind of Python iterator that will YIELD (instead of return)  
 contains an implicit next method. By definition, is a generator.  
 def gen\_naturals():  
 current = 0  
 while True:  
 yield current  
 current += 1  
 >>> gen = gen\_naturals()  
 >>> gen  
 <generator object... >  
 >>> next(gen)  
 0

the next = next method. it's an object. it's a generator. it doesn't need next. it's implicit. it's a generator. it's a generator. it's a generator.

Streams are similar to lists  
 def make\_fib\_stream():  
 return fib\_stream\_generator(0, 1)  
 def fib\_stream\_generator(a, b):  
 def compute\_rest():  
 return fib\_stream\_generator(b, a+b)  
 return stream(a, compute\_rest)

s.rest returns Stream(5, <... >)  
 usually → just have compute\_rest  
 like map\_stream(fn, s.rest)  
 return stream(fn(s.first), compute\_rest)

**Recursion** Tail recursion: (define (last s) (=cdrs) nil) (car s) (last (cdr s)))

**CONSTANT SPACE** (define (reverse-iter s result) (if null? s) result (reverse-iter (cdr s) (cons (car s) result))))

helper funcs are help fun

```

def remove_vowels(s):
  if len(s) == 0:
    return s
  return "" if s[0] in ('a', 'e', ...) else s[0] + remove_vowels(s[1:])

def merge(s1, s2):
  if len(s1) == 0:
    return s2
  if len(s2) == 0:
    return s1
  elif s1[0] < s2[0]:
    return s1[0] + merge(s1[1:], s2)
  else:
    return s2[0] + merge(s1, s2[1:])
  
```

r-lists: r = rlist(1, rlist(2, rlist(3, empty-list)))

r.first, r[0] r.rest, r[1] → returns rlist obj. r[1] returns 2

range = ending val - starting val  
tuple(range(0, 4)) → (0, 1, 2, 3)

gcd(a, b) == gcd(b, a % b)

```

def gcd-rec(a, b):
  if a < b:
    return gcd-rec(b, a)
  if a > b and not a % b == 0:
    return gcd-rec(b, a % b)
  return a

def gcd-iter(a, b):
  if a < b:
    return gcd-iter(b, a)
  while a > b and not a % b == 0:
    a, b = b, a % b
  return b
  
```

**EVAL/READ: Read-Eval-Print Loop.**

tokenize & parse → data structures into values → prints

**SCHEME EVAL:** takes in (expr, env) returns db-obj-form or scheme-apply returns procedure

**EVAL:** Base cases: primitive values (#s), look up values bound to symbols. Recursive calls: E val (operands) of call exp. Apply (op, arg) Eval (sub-exp) of special forms.

Base cases: Built-in primitive procedures. Rec. calls: Eval (body) of user defined proc.

new env. for user defined

→ mutually recursive. Eval required if call exp. encountered. Apply uses eval to evaluate operand exp. into args, and evaluate body of user-defined procedure. the recursion ends with language primitives.

**SCHEMES LISTS:** (1.2), valid list of schm tokens

```

def mutable_list():
  contents = empty-list
  def dispatch(message, value=None):
    nonlocal contents
    if message == 'len':
      return len-list(contents)
    elif message == 'get-item':
      return get-item(contents, val)
    elif message == 'push-first':
      contents = make-list(val, contents)
    elif message == 'pop-first':
      f = first(contents)
      contents = rest(contents)
      return f
    elif message == 'str':
      return str(contents)
    return dispatch
  return dispatch
  
```

mutable objects can change over execution of program

Complex facts: (fact 'conclusion') ('hypothesis1') ('hypothesis2')

**PARSING** reads string → returns valid scheme tokens

```

read > 42
42
read > '(123)
(quote (1 2 3))
read > nil
()
read > '()
(quote ())
read > '(1(23)(4(5)))
(1(23))(4(5))
read > '(hi there cs. (student))
(hi there cs student)
  
```

calculator: (+ 2 4 6 8) eval: 5 apply: 1 NOT SAME AS SCHEMES  
(+ 2 (\* 4 -6 8)) eval: 7 apply: 3

try: return x \* x except Type Error: print('incorrect arg type')

**Trees**

Tree(3, Tree(4), Tree(-2, Tree(8)), Tree(3))

ROOT (3) nodes (point in tree w/value) LEAF (8, 3)

```

def find_path(t, entry):
  if t is None or (t.is-leaf and t.entry != entry):
    return False
  elif t.entry == entry:
    return (entry, )
  else:
    left_path = find_path(t.left, entry)
    if left_path:
      return (t.entry, ) + left_path
    right_path = find_path(t.right, entry)
    if right_path:
      return (t.entry, ) + right_path
    return False
  
```

def are-siblings(s1, s2): if s1.is-leaf() and s2.is-leaf(): return False else: child names = [tree.child for tree in t.children for c in tree.children if s1 in child.names and s2 in child.names]: return True else: return False

**Env. diagram** Tips: when copying integers, just their values. if lists, just copy the arrow to point to that object (same thing) lambda - no binding nonlocal → no new val

when assign something like a = fun(15) then call a('sleepy')(5) earlier goes in global frame

**ORDERS OF GROWTH**

- Tree recursion is usually exponential  $O(b^n)$  & recursive fib()
- Increasing problem scales  $R(n)$  by factor  $O(n^c)$  for...
- factorial(n): if n=0: return 1 return factorial(n) + factorial(n-2)
- linear growth  $O(n)$  if just scale w/n
- fast-exp(b, n): if n=0: return 1 if n % 2 == 0: return sq-fast-exp(n/2) else: return b \* fast-exp(b, n-1)
- while with in while like def bis(n):  $\theta(n^2)$  while i <= n: sum += bis(n) return sum
- def subsets(n): if n==0: return [(1)] else: result = subsets(n-1) return result + [subset in result for subset in result.append(n)]

Simple tree recursive fib:

```

def fib(n):
  if n == 1:
    return 0
  elif n == 2:
    return 1
  else:
    return fib(n-1) + fib(n-2)
  
```

fib(4) fib(3) fib(2) fib(1) fib(1)

**BST: Binary Search Trees**

```

def right-is-bigger(bst):
  if not bst.left.is-empty and not bst.right.is-empty:
    return bst.right.size > bst.left.size
  return bst.left == empty_bst
  
```

def coerce(tree): "dispatch dict. repping tree" if tree is None: return None return { 'entry': tree.entry, 'left': coerce(tree.left), 'right': coerce(tree.right) }