

# MIDTERM 2

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$$\log n < n < n \log n < n^2$$

- Balanced search trees better because reinforce  $n \log n$  runtime
  - o Binary search trees don't
- Trees
  - o Preorder: roots first, depth first, left to right
  - o Postorder: children first, breadth first
  - o Inorder: children first, depth first

Handwritten notes on a piece of paper:

$$\begin{aligned} 1 \leq \text{leaves} &\leq 2^h \\ h \leq \text{internal nodes} &\leq 2^h - 1 \\ \log_2(n+1) - 1 \leq h &\leq n - 1 \\ \therefore \text{For complete tree,} \\ \text{there are } 2^{\log_2(n+1)-1} &= \frac{n+1}{2} \approx \frac{n}{2} \text{ leaves} \end{aligned}$$

- o Runtime are between  $n$  and  $\log n$  depending on balanced or branched.

```
/** Node in T containing L,
 * or null if none */
static BST find(BST T, Key L) {
    if (T == null)
        return T;
    if (L.keyequals (T.label()))
        return T;
    else if (L < T.label())
        return find(T.left(), L);
    else
        return find(T.right (), L);
}

/** Insert L in T, replacing existing
 * value if present, and returning
 * new tree. */
BST insert(BST T, Key L) {
    if (T == null)
        return new BST(L);
    if (L.keyequals (T.label()))
        T.setLabel (L);
    else if (L < T.label())
        T.setLeft(insert (T.left (), L));
    else
        T.setRight(insert (T.right (), L));
    return T;
}
```

- Queues and Stacks
  - o Stacks: dishes
    - Push, pop
  - o Queues: first in, first out
    - Enqueue, dequeue
    - Front
  - o Constant time
  - o Priority queue
    - Insert
    - Use key
  - o Heap
    - Sorted by min/max/etc.
    - Each level needs to be filled up first
    - Can be represented as array
    - Compare/swap
    - Stick in new spots and bubble up(remove)/down(insert) until property satisfied
- Hash tables
  - o Constant time for inserting, over linkedlist
  - o chaining